

# A New Diode Rectifier Type Utility Interface with Clean Power Characteristics

Sewan Choi and Prasad N. Enjeti

## Abstract

In this paper, a new active interphase reactor for twelve-pulse diode rectifiers is proposed. In this scheme, a low kVA (0.02  $P_o$  (PU)) active current source injects a triangular current into an interphase reactor of a twelve-pulse diode rectifier. The proposed system draws near sinusoidal input currents from the utility with less than 1% THD is suitable for powering larger kVA ac motor drive systems. Detailed analysis of the proposed scheme along with design equations is illustrated. Simulation results verify the concept. Experimental results are provided from a 208V, 10kVA diode rectifier system.

## I. Introduction

Large harmonics, poor power factor and high total harmonic distortion (THD) in the utility interface are common problems when nonlinear loads such as adjustable speed drives, power supplies, induction heating systems, UPS systems and aircraft converter systems are connected to the electric utility. In several cases, the interface to the electric utility is processed with a three phase uncontrolled diode bridge rectifier. Due to the nonlinear nature of the load, the input line currents have significant harmonics. For adjustable speed ac motor drive systems with no dc-link smoothing inductor, the discontinuous conduction of the diode bridge rectifier results in a high THD and can lead to the malfunction of sensitive electronic equipment. The recommended practice, IEEE 519, has evolved to maintain utility power quality at acceptable levels [1].

A number of methods have been proposed to overcome the presented problems [2-12]. One approach is to use a conventional twelve-pulse diode rectifier which requires two six-pulse diode rectifiers connected via Y- and Y-Y transformers.

An interphase reactor is required to ensure the independent operation of the two parallel-connected three-phase diode bridge rectifiers. The operation of the conventional twelve-pulse diode rectifier results in the cancellation of the 5th and 7th harmonics in the input utility line currents. To increase

the pulse number further to 18 or 24, additional diode bridge rectifiers along with complicated multiphase transformer arrangements become necessary, which adds to the cost and complexity.

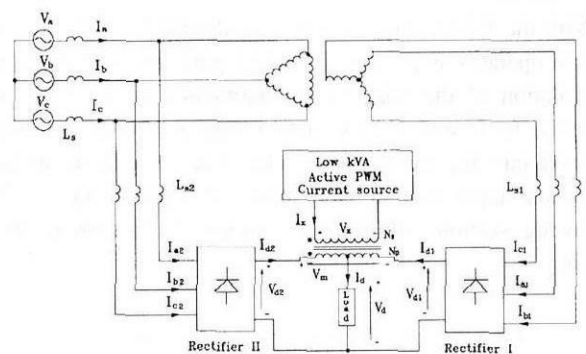


Fig. 1. Circuit diagram of the proposed clean power utility interface. Current  $I_a$  is near sinusoidal in shape with less than 1% THD.

This paper proposes a new three-phase diode rectifier system which draws near sinusoidal input currents from the three phase electric utility. In the proposed approach shown in Fig. 1, a transformer of 0.52  $P_o$  (PU) capacity is employed. The interphase reactor and the line impedances  $L_{s1}$ ,  $L_{s2}$  are designed such that stable twelve-pulse operation is obtained with equal current sharing. A low kVA (0.02  $P_o$  (PU)) PWM-controlled active current source,  $I_x$  is injected into the secondary winding of the interphase reactor. It is shown via rigorous mathematical modeling as well as computer simulations that the exact shape of  $I_x$  shown in Fig. 3 (a) can be computed to alter the utility line current  $I_a$  to

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S.W. Choi is with Samsung Electro-Mechanics.

P.N. Enjeti is with Department of Electrical Engineering, Texas A&M University.

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a perfect sinewave. It is further shown that an approximation to the exact waveshape of  $I_x$  is a triangular wave shown in Fig. 4 (a). Therefore by injecting a triangular shaped current  $I_x$  into the secondary winding of the interphase reactor, near sinusoidal input line currents flow in the utility line with less than 1% THD. This results in high performance with reduced kVA components and offers clean power utility interface suitable for powering larger kVA ac motor drives. Detailed analysis of the proposed schemes is discussed.

## II. Proposed Clean Power Utility Interface

Fig. 1 shows the circuit diagram of the proposed scheme to shape input line currents. The main transformer has delta-wye winding ( kVA rating of  $0.52 P_o$  (PU) ) with a  $\sqrt{3}$  to 1 turns ratio to maintain an equal per unit voltage. They are connected in such a way that the two diode bridge rectifiers have balanced sets of three-phase voltages with 30 degrees phase shift. The proposed system is identical to a conventional 12-pulse system except that the interphase reactor has an additional winding. The additional winding is used to inject a low kVA PWM current source to shape input line current.

With the PWM current source,  $I_x$ , disabled (i.e.  $I_x = 0$ ) the system operates as a conventional 12-pulse rectifier providing cancellation of the 5th and 7th harmonics in the input line currents,  $I_a$ ,  $I_b$  and  $I_c$ . The active current source  $I_x$ , when injected into the interphase reactor (Fig. 1), results in near sinusoidal input current with unity input power factor. The following sections illustrate the proposed concept in more detail.

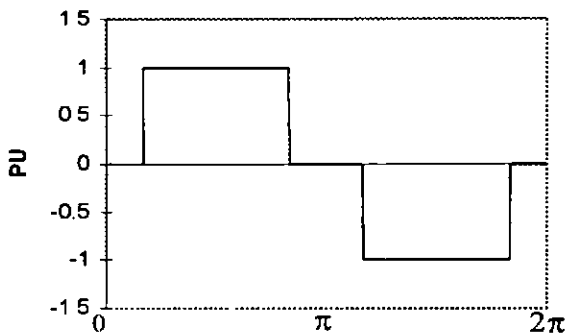


Fig. 2. Switching function  $S_{a1}$  for Rectifier I in Fig. 1.

### A. Analysis of the proposed active interphase reactor

Fig. 1 shows the proposed active interphase reactor for a 12-pulse diode rectifier. In this section, waveforms are analyzed to determine the relationship between current  $I_x$  and

input currents  $I_a$ ,  $I_b$  and  $I_c$ . With  $I_x = 0$ , input current  $I_a$  can be shown to be [2,5],

$$I_a = I_{a2} + \frac{1}{\sqrt{3}} (I_{a1} - I_{c1}) \quad (1)$$

Equation (1) describes a 12-pulse input line current with 5th and 7th harmonics absent and

$$I_{d1} = I_{d2} = \frac{1}{2} I_d \quad (2)$$

An active current  $I_x$  is now injected into the secondary winding of the interphase reactor as shown in Fig. 1. Fig. 6 shows the circuit topology for implementing this scheme. Analyzing the MMF relationship of the interphase reactor, we have,

$$N_p (I_{d2} - I_{d1}) = N_s I_x \quad (3)$$

where  $N_p$  and  $N_s$  are the numbers of turns of the primary and the secondary windings of the interphase reactor. The load current  $I_d$  is,

$$I_d = I_{d1} + I_{d2} \quad (4)$$

From (3) and (4) we have,

$$I_{d1} = \frac{1}{2} (I_d - \frac{N_s}{N_p} I_x)$$

$$I_{d2} = \frac{1}{2} (I_d + \frac{N_s}{N_p} I_x) \quad (5)$$

Fig. 2 shows switching function  $S_{a1}$  for phase a of Rectifier-I shown in Fig. 1. The Fourier series expansion for  $S_{a1}$  is given by,

$$S_{a1}(\omega t) = \frac{2\sqrt{3}}{\pi} \left( \sin \omega t - \frac{1}{5} \sin 5\omega t - \frac{1}{7} \sin 7\omega t + \frac{1}{11} \sin 11\omega t + \frac{1}{13} \sin 13\omega t \dots \right) \quad (6)$$

and for phase b and c, the switching functions can be written as,

$$\begin{aligned} S_{b1} &= S_{a1} \angle -120^\circ \\ S_{c1} &= S_{a1} \angle +120^\circ \end{aligned} \quad (7)$$

Similarly, the switching functions for Rectifier-II in Fig. 1 with a 30 degree phase shift are,

$$\begin{aligned} S_{a2} &= S_{a1} \angle -30^\circ \\ S_{b2} &= S_{b1} \angle -30^\circ \\ S_{c2} &= S_{c1} \angle -30^\circ. \end{aligned} \quad (8)$$

The input currents for Rectifier I and II can now be expressed in terms of switching functions as,

$$\begin{bmatrix} I_{a1} \\ I_{b1} \\ I_{c1} \end{bmatrix} = \begin{bmatrix} S_{a1} \\ S_{b1} \\ S_{c1} \end{bmatrix} I_{d1} \quad (9)$$

and



$$\begin{bmatrix} I_{a2} \\ I_{b2} \\ I_{c2} \end{bmatrix} = \begin{bmatrix} S_{a2} \\ S_{b2} \\ S_{c2} \end{bmatrix} I_{d2} \quad (10)$$

Equation (1) can now be modified using (5) and the switching functions described in (6)-(10) as,

$$I_a = \frac{1}{2\sqrt{3}} (S_{a1} - S_{c1}) \cdot (I_d - \frac{N_s}{N_p} I_x) + \frac{1}{2} S_{s2} (I_d + \frac{N_s}{N_p} I_x) \quad (11)$$

Equation (11) illustrates the relationship between  $I_x$  and input current  $I_a$ . For input current  $I_a$  to be sinusoidal,

$$I_x = \frac{N_p [2I_{a,1} - I_d \left\{ \frac{S_{a1} - S_{c1}}{\sqrt{3}} + S_{a2} \right\}]}{N_s \left\{ \frac{S_{c1} - S_{a1}}{\sqrt{3}} + S_{a2} \right\}} \quad (12)$$

Note  $I_a$  is replaced by  $I_{a,1}$ , where  $I_{a,1}$  is the fundamental component of  $I_a$ . Therefore, equation (12) describes the exact shape of  $I_x$  for a given load current  $I_d$ . Since input power is equal to output power, we have

$$\sqrt{3} V_{LL} |I_{a,1}| = V_d I_d \quad (13)$$

where  $V_d = 1.35 V_{LL}$  and  $V_{LL}$  is the line to line rms voltage and  $|I_{a,1}|$  is rms value of  $I_{a,1}$ .

Hence, from (13) we have,

$$|I_{a,1}| = 0.7794 I_d \quad (14)$$

Now, for input current  $I_a$  to be sinusoidal, i.e.,

$$I_a = \sqrt{2} |I_{a,1}| \sin \omega t \quad (15)$$

Fig. 3 (a) shows the shape of  $I_x$  for sinusoidal input current.

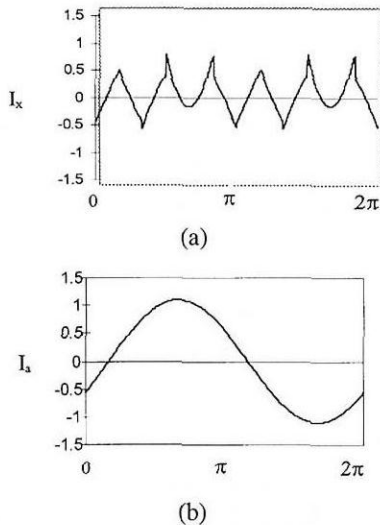


Fig. 3. (a) Injected current  $I_x$  calculated from (12)  
(b) Input line current  $I_a$  (pure sinusoidal).

#### B. Simulation results of the proposed approach

The proposed active interphase reactor approach shown in

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Fig. 1 is simulated on SABER and the results are presented in this section. From Fig. 3 (a), it is apparent that  $I_x$  is near triangular in shape. Simplifying the injected current  $I_x$  to a triangular wave shape (Fig. 4(a)) yields a near sinusoidal input current  $I_a$  (Fig. 4 (c)). Furthermore, generating a triangular injection current  $I_x$  into the secondary of the interphase reactor can be accomplished by means of a PWM-controlled current source (Fig. 6). Fig. 4 (b) shows the input current of the rectifier blocks  $I$  (Fig. 1) as a result of the injected current  $I_x$ . Fig. 5 (a) and (b) show the dc output voltages  $V_{d1}$  and  $V_{d2}$ . Fig. 5 (c) shows the voltage across the interphase reactor.

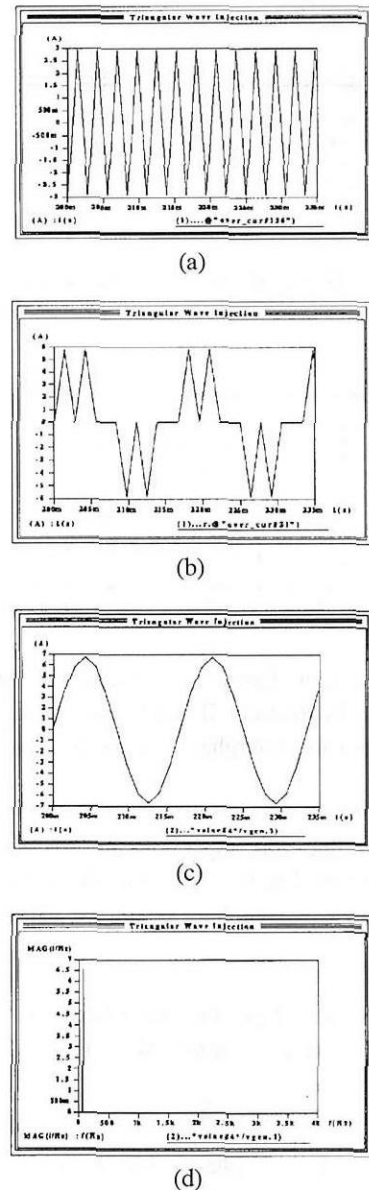
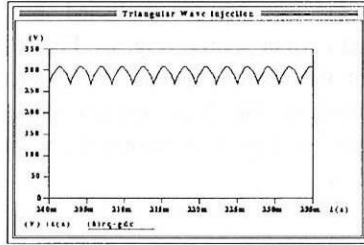


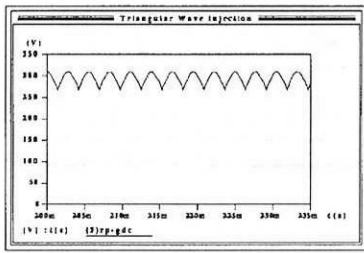
Fig. 4. Simulation results.

(a) Injected current  $I_x$  (b) Rectifier I input current  $I_{a1}$  (c) Input line current  $I_a$  (d) Frequency spectrum of  $I_a$

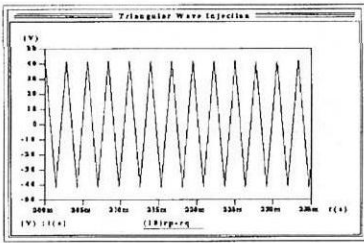
It should be noted that injecting active current  $I_x$  (Fig. 4 (a)) which is triangular in shape yields near sinusoidal input currents (Fig. 4 (c)) of less than 1% THD. The kVA rating of the injected current is small and is computed in the next section.



(a)



(b)



(c)

**Fig. 5.** Simulation Results (a) Rectifier I output voltage  $V_{d1}$ . (b) Rectifier II output voltage  $V_{d2}$ . (c) Voltage across the interphase reactor  $V_m = V_{d2} - V_{d1}$ .

### C. kVA rating of the injected current source, $I_x$

The line to line rms input voltage  $V_{LL}$  and dc output current  $I_d$  is assumed to be 1 per unit. The voltage across the interphase reactor  $V_m$  (see Fig. 1) can be expressed as,

$$V_m = V_{d2} - V_{d1}. \quad (16)$$

Fig. 5 (a) and (b) show the waveshape of  $V_{d1}$  and  $V_{d2}$ . Furthermore,  $V_{d1}$  can be expressed in Fourier series as [3],

$$V_{d1} = \sqrt{2} V_{LL} \frac{6}{\pi} \sin \frac{\pi}{6} \left( 1 - \sum_{n=6,12,18,\dots}^{\infty} \frac{2}{n^2 - 1} \cos \frac{n\pi}{6} \cos n\omega t \right) \quad (17)$$

Output voltage  $V_{d2}$  is phase shifted by 30 degree. By substituting (17) into (16),  $V_m$  can be expressed as,

$$V_m = -5.4018 V_{LL} \sum_{n=6,12,18,\dots}^{\infty} \frac{1}{n^2 - 1} \cos \frac{n\pi}{6} \sin \frac{n\pi}{12} \sin(n\omega t - \frac{\pi}{12}) \quad (18)$$

From (18), the rms value of  $V_m$  can be computed as,

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$$V_{m,ms} = 0.1098 V_{LL} \quad (19)$$

The voltage across the interphase reactor secondary winding  $V_x$  is given by,

$$V_x = \frac{N_s}{N_p} V_m. \quad (20)$$

Then, from (19) and (20) the rms value of  $V_x$  is,

$$V_{x,ms} = 0.1098 V_{LL} \frac{N_s}{N_p}. \quad (21)$$

From the results in the previous section, the peak value of the current  $I_x$  of Fig. 4 (a) is  $0.5 I_d$ . Therefore, the rms value of  $I_x$  for a triangular waveshape is,

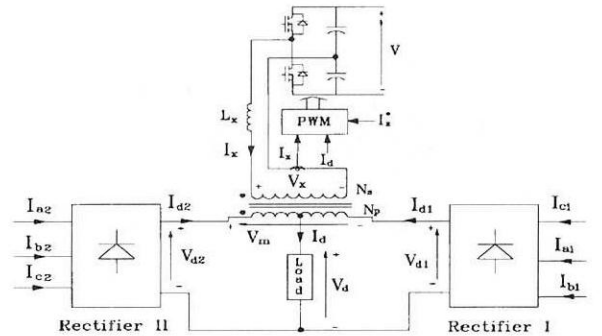
$$I_{x,ms} = \frac{0.5}{\sqrt{3}} I_d \frac{N_p}{N_s} = 0.2887 I_d \frac{N_p}{N_s} \quad (22)$$

The rms value of  $I_x$  can be reduced by adjusting turns ratio  $N_p/N_s$  between the primary and the secondary windings of the interphase reactor.

From (21) and (22), the kVA rating of the injected current source,  $kVA_{INV}$ , can be computed as,

$$\begin{aligned} kVA_{INV} &= V_{x,ms} \cdot I_{x,ms} \\ &= 0.0227 P_o \text{ (PU)} \end{aligned} \quad (23)$$

Equation (23) shows that the kVA rating of the injected current source  $I_x$  is a small percentage of the output power. This demonstrates the superior features of the proposed scheme to realize a clean power utility interface.



**Fig. 6.** Circuit diagram for implementation of the proposed schemes.

### D. Implementation of the active current source $I_x$

Fig. 6 shows the circuit diagram for implementing the proposed scheme. Injected current  $I_x$  shown in Fig. 4 (a) is generated from a current controlled PWM inverter.

Block diagram of the gating signal generator for the PWM inverter is shown in Fig. 7. The reference for the injected current is synchronized with the input voltages. Injected current  $I_x$  is fed back to the gating signal generator and the current error is compared to a triangular carrier wave



(25kHz) to generate the PWM gating signals for the inverter switching devices. As the magnitude of output dc current  $I_d$  changes, the magnitude is fed back and multiplied by the injected current to make the reference  $I_x^*$ .

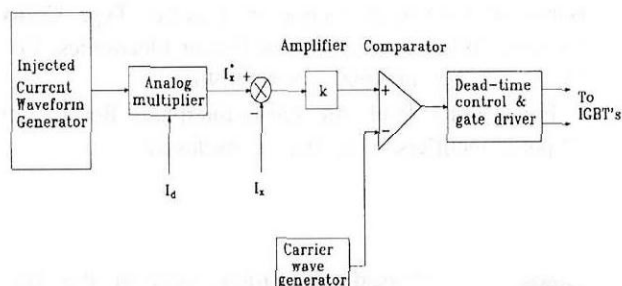


Fig. 7. Block diagram of the current-controlled PWM gating signal generator.

### III. Experimental Results

A 208V, 10kVA diode rectifier system employing the proposed scheme has been implemented in the laboratory. The interphase reactor employed in the experiment was designed with the turns ratio of  $N_p : N_s = 1 : 2$ .

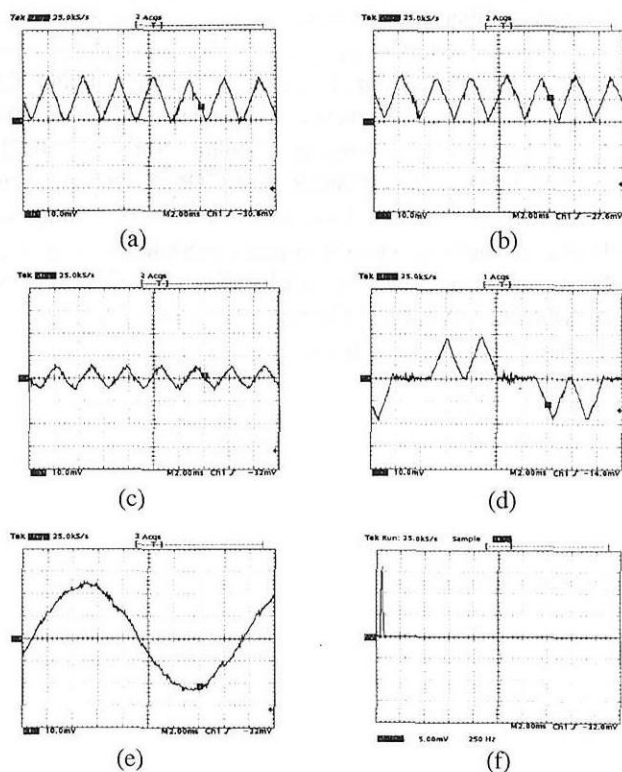


Fig. 8. Experimental results (5A/Div.)

- (a) Output current  $I_{d1}$ . (b) Output current  $I_{d2}$ . (c) Injected current  $I_x$ . (d) Rectifier input current  $I_{a1}$ . (e) Input line current  $I_a$  (f) Frequency spectrum  $I_a$ .

Fig. 6 shows the experimental setup to verify the operation of proposed system. Fig. 8 shows the experimental results obtained. Fig. 8 (c) shows the injected current  $I_x$  and Fig. 8 (a) and (b) show the resulting rectifier output currents  $I_{d1}$  and  $I_{d2}$ , respectively. Fig. 8 (d) shows the rectifier input current  $I_{a1}$ . Finally, the experimental utility input current  $I_a$  and its frequency spectrum are shown in Fig. 8 (e) and (f), respectively. Experimental results show good agreement between theory and practice and demonstrate clean power characteristics of the proposed scheme.

### IV. Conclusion

In this paper a new active interphase reactor for a twelve-pulse rectifier system has been proposed. It has been shown that by injecting a low kVA(0.02  $P_o$  (PU)) active current source  $I_x$  into the interphase reactor near sinusoidal input currents with less than 1% THD can be obtained. The proposed system is a high performance clean power utility interface suitable for powering larger kVA ac motor drive systems. Detailed analysis of the proposed scheme along with design equations has been illustrated. Simulation results have been shown to verify the proposed concepts. Experimental results have been provided from a 208V, 10kVA rectifier system.

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**Sewan Choi** was born in Seoul, Korea, on March 3, 1963. He received the B.S. Degree in electronic engineering in 1985 from Inha University in Incheon, Korea and the M.S. and Ph.D. degrees in electrical engineering in 1992 and 1995, respectively, from Texas A&M University, College Station, TX. From 1985 to 1990, he was with Daewoo

Heavy Industries, where he was involved in the development of several industrial controllers. He is currently a Senior Researcher working on the development of Intelligent Power Modules in Samsung Electro-Mechanics, Suwon, Korea. His research interests include clean power utility interface and design and control of advanced power converters.



**Prasad N. Enjeti** received the B.E. degree from Hyderabad, India, in 1980, the M.Tech. degree from Indian Institute of Technology, Kanpur, in 1982, and the Ph.D. degree from Concordia University, Montreal, Canada, in 1987, all in electrical engineering. He then joined the Electrical Engineering Department at Texas A&M University,

College Station, where he is currently an Associate Professor. His current research interest include advance converters for power supplies and motor drives, power quality issues and active power filter development, utility interface issues and "clean" power converter designs, and electronic ballasts for fluorescent HID lamps. Dr. Enjeti is Transactions Editor for the Industrial Power Converter Committee (IPCC) of the IEEE IAS and an Associate Editor for the IEEE TRANSACTIONS ON POWER ELECTRONICS. He was the recipient of the IEEE-IAS second best paper award in 1993 and second best transaction paper published in mid-year 1994 to mid-year 1995 in IEEE TRANSACTIONS ON INDUSTRIAL APPLICATIONS. He is a registered Professional Engineer in Texas.